

Unit 2 BIG QUIZ - Derivatives

For the problem below use *either* definition of the derivative to find the derivative (2 points).

1. $y = \sqrt{x}$ 1. _____

2. (2 points) If $f(x) = 10x^2$, find $f'(-1) =$ 2. _____
 a) -20 b) -10 c) 10 d) 20

Find the derivatives for the following (3 points each):

3. $y = 4x^2 + \cos x$ 4. $y = \sqrt{\sin x}$ 3. _____

4. _____

5. $y = x^3 \tan x$ 6. $y = \frac{x-5}{x+5}$ 5. _____

6. _____

7. $y = \frac{1}{x^4} - \frac{1}{x} + x^3$ 8. $y = x^4 \sqrt{x+1}$ 7. _____

8. _____

9. If $f(x) = (4x)^{5/2}$, find $f'(1) =$ 10. $y = \sin(6x-1)$ 9. _____

10. _____

Use the following table for 11-13. (2 points each)

| x | $f(x)$ | $f'(x)$ | $g(x)$ | $g'(x)$ |
|-----|--------|---------|--------|---------|
| 0 | 2 | 0 | 1 | 1 |
| 1 | 3 | 2 | 3 | 2 |
| 2 | 4 | 1 | -5 | 1 |

11. If $h(x) = f(x) \cdot g(x)$, find $h'(1) =$

- a) 36 b) 13 c) 12 d) 0

11. _____

12. If $h(x) = f \circ g(x)$, find $h'(0) =$

- a) 2 b) 4 c) 6 d) 8

12. _____

13. If $h(x) = \frac{f(x)}{g(x)}$, find $h'(2) =$

- a) $-\frac{4}{5}$ b) $-\frac{9}{25}$ c) $-\frac{1}{25}$ d) $-\frac{1}{5}$

13. _____

14. Find $\frac{dy}{dx}$ for the following (use implicit differentiation) (5 points):

$$4xy + 3x^3y^2 = 20$$

14. _____

15. Find the slope of the curve $y = 3x^3 - 7x^2 + 12x + 1$ at $x = 1$ (3 points)

15. _____

16. Find the slope of the tangent line of $x^2 + 3xy + y^2 = 11$ at the point $(1, 3)$ (4 points)

16. _____

17. Find the equation of the tangent line of $y = x^2 + 3x - 4$ at $x = 2$. (4 points) 17. _____

18. Find the value(s) of the horizontal tangent(s) for $y = 2x^3 - 3x^2 - 12x + 20$. (4 points) 18. _____

19. Find the second derivative for $y = \frac{x^3}{6} - 9x^2 + 6x - 5$. (4 points) 19. _____

Find the derivatives for the following (4 points each):

20. $g(x) = \left(\cos\left(\frac{x}{2}\right) \right)^4$

21. $y = \sin^3(\sqrt{x})$

20. _____

21. _____

22. $y = e^{\cos(8x)}$

22. _____

Bonus: At what point is the tangent to the curve $y = 2x^2$ parallel to the line $y - 12x - 10 = 0$ (2 points)

Bonus: _____