

The Mean Value Theorem (4.3)

Mean Value Theorem

Let f be a function that satisfies the following hypotheses:

1. f is continuous on the closed interval $[a, b]$
2. f is differentiable on the open interval (a, b)

Then there is a number c in (a, b) such that $f'(c) = \frac{f(b) - f(a)}{b - a}$

Verify that the function satisfies the hypotheses of the **Mean Value Theorem** on the given interval. Then, find all numbers c that satisfy the conclusion of the **Mean Value Theorem**.

1. $f(x) = 2x^3 - 5x^2 + 1$ $[0, 2]$

2. $f(x) = 2x\sqrt{x+4}$ $[-8, -4]$

$f(x) = 2x\sqrt{x+4}$ $[-4, 0]$

3. $f(x) = \frac{2x}{x-2}$ $[0, 4]$

$f(x) = \frac{2x}{x-2}$ $[3, 6]$

Use the First Derivative Test to find the critical points and the intervals on which the function is increasing/decreasing.

4. $f(\theta) = \theta - 2\cos\theta \quad [0, 2\pi]$

5. $f(x) = \frac{x^3}{x^2 - 3}$

5. $f(x) = x^{5/2} - x^2 \quad (0, \infty)$